NUMERICAL SIMULATION OF THE FLOW AROUND A WIND WHEEL WITH ROTATING CYLINDRICAL BLADES

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The article discusses the results of numerical simulation of the flow around a wind wheel with blades in the form of rotating cylinders using the software package ANSYS. The advantage of a wind turbine with rotating cylindrical blades in comparison with traditional blade installations is the starting moment and the beginning of energy production at a wind speed of (2 - 3) m/s. A mathematical model has been developed based on three-dimensional Navier-Stokes equations in a rotating system. The corresponding boundary conditions are formulated. A calculated pattern of the flow around the wind wheel with rotating cylindrical blade is obtained. There are shown regions of the velocity field with turbulent vortices, which are formed at high Reynolds numbers. The degree of influence of the angular speed of rotation of the wind wheel on the magnitude of the moment of forces at various speeds of the incoming air flow has been determined.

Keywords: wind wheel, ANSYS, rotating cylinder, mathematical model, moment of forces.

Introduction

Experimental research of a wind power plant is a rather time-consuming process, and requires certain climatic conditions with wind components. In such cases, it is advisable to use a theoretical study using mathematical modeling [1]. A wind power plant with rotating cylinders is distinguished by the Magnus effect involved in its operation from existing blade wind turbines. The Magnus force that occurs on a rotating cylinder due to the asymmetry separation of the flow from its surface can be an order of magnitude higher than the lifting force of the traditional blade. Based on this, in the case of the installation under consideration, we can expect an increase in the driving force of the wind wheel, as well as other operational advantages. One of the main advantages of a wind power plant with cylindrical blades is the start of energy generation at low wind speeds starting from 2 m/s, in contrast to the blades with 5 m/s [2].

1. The mathematical model of a wind wheel

1.1. System of equations

In the simulation of rotation, the three-dimensional Navier-Stokes equations in a rotating frame of reference have the form:

\[
\frac{\partial \rho}{\partial t} + \nabla \cdot \rho \mathbf{v} = 0, \tag{1}
\]
conservation of momentum equation

\[
\nabla \cdot \left( \rho \left( \vec{v} \cdot \nabla \vec{v} \right) \right) + \rho \left( 2 \vec{\omega} \times \vec{v} + \vec{\omega} \times \nabla \times \vec{r} \right) = -\nabla p + \nabla \tau ,
\]

(2)

where \( \rho \) – air density; \( \vec{v} \) – relative speed; \( \vec{\omega} \) – angular velocity; \( \vec{\omega} \times \vec{v} \) – coriolis acceleration; \( \vec{\omega} \times \nabla \times \vec{r} \) – centripetal acceleration; \( \tau \) – viscous stress; \( p \) – pressure.

Since the simulation of a rotating wind wheel involves non-stationary aerodynamic effects, choosing the right turbulence model is of great importance. The realizable k-\( \varepsilon \) turbulence model was used to model the currents around the rotating wind wheel. This model is used to model single-phase flows at high Reynolds numbers. The physical interface is suitable for incompressible flows, weakly compressible flows, and compressible flows at low M (Mach number), usually M less than 0.3).

The main assumptions made when describing the flow of air flowing around a wind power plant:
1. Due to the low values of M, when the ratio of the gas velocity to the local speed of sound M<<0.1, the motion of the air flow is described by the equations valid for an incompressible medium.
2. Due to the large Re (the ratio of the inertial forces to the viscosity forces, Re >10^4), the flow is turbulent.
3. Due to the low values of M and slight temperature changes in the vicinity of the wind wheel, the flow is isothermal.

The equations implemented at the k-\( \varepsilon \) interface for solving turbulent flow problems include the Navier-Stokes equations (RANS) averaged by Reynolds for momentum conservation and the continuity equation for mass conservation (3). The flow near the walls is modeled using wall functions \( f_i \).

\[
\frac{\rho \vec{u}_j}{\overline{\rho}} = \frac{\rho \vec{f}_i}{\overline{\rho}} + \frac{\partial}{\partial x_j} \left[ -\overline{\rho \delta_i} + \mu \left( \frac{\partial \vec{u}_i}{\partial x_j} + \frac{\partial \vec{u}_j}{\partial x_i} \right) - \rho \overline{\mu ' u_j^j} \right],
\]

(3)

where \( \rho \vec{f}_i \) – external forces; \( \overline{\rho \delta_i} \) – pressure forces; \( \mu \left( \frac{\partial \vec{u}_i}{\partial x_j} + \frac{\partial \vec{u}_j}{\partial x_i} \right) \) – viscous forces; \( \rho \overline{\mu ' u_j^j} \) – Reynolds stresses.

The left-hand side of this equation is the change in the average momentum of the liquid element due to the instability of the average flow and the convection of the average flow. This change is balanced by the averaged external forces, pressure forces, viscous forces, and apparent stress \( \rho \overline{\mu ' u_j^j} \) due to the fluctuating velocity field, commonly referred to as the Reynolds stress. Equations (4 - 6) are an implementation of the k-\( \varepsilon \) turbulence model:

\[
\frac{\partial}{\partial t} (\rho k) + \frac{\partial}{\partial x_i} (\rho u_i k) - \frac{\partial}{\partial x_i} \left[ \mu + \frac{\mu}{\sigma_k} \frac{\partial k}{\partial x_i} \right] = G_k - \rho \varepsilon ,
\]

(4)

\[
\frac{\partial}{\partial t} (\rho \varepsilon ) + \frac{\partial}{\partial x_j} (\rho u_j \varepsilon ) = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu}{\sigma_\varepsilon} \right) \frac{\partial \varepsilon}{\partial x_j} \right] + \rho \varepsilon \left( C_1 S - C_2 \frac{\varepsilon}{k + \sqrt{\varepsilon}} \right),
\]

(5)

\[
\mu = p C_\mu \frac{k^2}{\varepsilon} ,
\]

(6)

where \( G_k \) – the turbulence kinetic energy of due to the average velocity gradients; \( k \) – is the turbulent kinetic energy; \( \varepsilon \) – turbulent dissipation; \( \mu \) – eddy viscosity; \( \sigma_k, \sigma_\varepsilon, C_1, C_2 \) – model constants (\( \sigma_k = 1.0, \sigma_\varepsilon = 1.2, C_1 = 1.44, C_2 = 1.9 \)); \( S = \sqrt{2 S_y S_y} \) – is the modulus of the strain rate tensor; \( C_\mu \) – dimensionless empirical constant.

1.2 Boundary conditions and computational model

To increase the computational efficiency, it was decided to use the symmetric and rotational nature of the wind turbine operation [9, 10]. Figure 1 shows the computational domain and the built - in grid with boundary conditions. The boundary conditions are presented in Table 1.
2. Discussion of numerical simulation results

As a result of numerical simulation, a picture of the air flow around the wind wheel was obtained (Figure 2). As can be seen from the figure, a three-dimensional vortex characteristic of a turbulent flow at high Reynolds numbers is observed in the rear part. This phenomenon is characterized by the constant distribution’s formation of air flow characteristics’s inconsistent pulsations in wavelength range from the minimum determined by the viscosity forces to the maximum determined by the flow conditions at the boundary. Studying the methods of numerical study of wind power plants, it was found that the result of modeling should be the dependences of mechanical parameters, namely:

1) The functional dependence of mechanical power on air flow parameters and speed:

\[ P_m = f(v, \eta) , \]
where $P_m$ – mechanical output power; $v$ – air flow rate; $n_1$ – the number of revolutions of the wind wheel.

2) The directly proportional dependence of the mechanical moment on the mechanical power:

$$M_m = \frac{P_m}{\omega},$$

where $M_m$ – mechanical moment; $\omega$ – the angular speed of rotation of the propeller.

3) The equation describing the motion of the wind wheel:

$$J \cdot \frac{dw}{dt} = M_m - M_g,$$

where $J$ – wind wheel moment of inertia; $M_g$ – useful moment load on the shaft [1, 6].

Fig. 2. Pictures of the flow around the wind wheel velocity field at $v = 15$ m/s: a) front view; b) rear view.

The above dependencies show the complete dynamic picture of the wind wheel. Figure 3 shows influence diagram of the equivalent concentrated forces $Q_v$, $Q_w$ and the force $F_g$, which forms the moment of the payload on the propeller shaft.

Fig. 3. Scheme of action of the resulting equivalent forces on the wind wheel:

$R$ – outer radius of the wind wheel; $r_g$ – force application shoulder $F_g$; $O$ – the axis of the wind wheel; $r$ – force application shoulder $Q_v$; $r_1$ – force application shoulder $Q_{wr}$.

The moments of forces affecting the propeller, relative to the axis of rotation, is the product of the above forces by the length of the shoulder (Fig.). Let's define the moments value:
\[ M_v = Q_v \cdot r_w \]

- the moment made by the air flow with a speed \( v \): 
\[ M_{wr} = Q_{wr} \cdot r_w \]

- the moment made by the payload of the wind turbine:
\[ M_g = F_g \cdot r_g \]

The total mechanical moment made by the blades of the propeller [1]:
\[ M_m = M_v - M_{wr} - M_g \]

where \( Q_w \) — force application shoulder \( r_w \); \( Q_{wr} \) — force application shoulder \( r_{w1} \); \( F_g \) — force application shoulder \( r_g \).

Figures 4 (a-d) show the effect of the speed of rotation of the wind turbine \( n_1 \) on the moment of forces \( M \) acting on the wind turbine for different speeds of the incoming flow \( v \) and different speeds of rotation of the cylinders \( n \). According to the given dependencies, it is possible to determine the speed of free rotation of the wind wheel, i.e. without taking into account the moment of friction forces in the bearings and the moment of forces arising in the generator. The nature of the linear dependence of the values of the moment of forces on the speed of free rotation of the wind wheel does not contradict the results [1] \( n_1 \), rpm.

As you can see, the results obtained with a sufficient degree of accuracy \((R^2 > 0.9972)\) are approximated by dependences of the form:
\[ n_1(n, v) = A(n)v^{B(n)}. \]
In this formula the free stream velocity is given in m/s, and the rotation speeds of the cylinder’s $n$ and $n_1$ in rpm. It can be shown that the functions $A(n)$ and $B(n)$ have the following form:

$$A(n) = 12.958n^{0.1224},$$
$$B(n) = 0.4483n^{0.0881}.$$

**Conclusions**

A mathematical model with the computational domain of the wind wheel has been developed using the ANSYS program. A picture of an air flow with a three-dimensional vortex characteristic of a turbulent flow at high Reynolds numbers is obtained. The dependences of the influence of the rotation speed of the wind turbine on the moment of forces acting on the wind wheel are numerically determined at various speeds of the incoming air flow and different speeds of rotation of the cylinders. It has been established that the magnitude of the wind wheel moment of forces increases in direct proportion to the revolutions number of rotating cylinder and the angular velocity of the wind wheel. It should be noted that the results obtained are valid within the framework of given mathematical model with the accepted assumptions and boundary conditions.

**REFERENCES**

9. ANSYS Fluent software. Available at: www.ansys.com/products/fluids/ansys-fluent

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